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McClear: a new model estimating downwelling solar radiation at
ground level in clear-sky conditions

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Abstract. A new fast clear-sky model called McClear was developed to estimate the downwelling shortwave direct and
global irradiances received at ground level under clear skies. It is a fully physical model replacing empirical relations or
simpler models used before. It exploits the recent results on aerosol properties, and total column content in water vapour
and ozone produced by the MACC project (Monitoring Atmosphere Composition and Climate). It accurately reproduces the irradiance computed by the libRadtran reference radiative transfer model with a computational speed approximately $10^5$ times greater by adopting the abaci, or look-up
table, approach combined with interpolation functions. It is therefore suited for geostationary satellite retrievals or numerical weather prediction schemes with many pixels or grid points, respectively. McClear irradiances were compared to 1 min measurements made in clear-sky conditions at several stations within the Baseline Surface Radiation Network in various climates. The bias for global irradiance comprises between $-6$ and $25$ W m$^{-2}$. The RMSE ranges from $20$ W m$^{-2}$ (3 \% of the mean observed irradiance) to $36$ W m$^{-2}$ (5 \%) and the correlation coefficient ranges between 0.95 and 0.99. The bias for the direct irradiance comprises between $-48$ and $+33$ W m$^{-2}$. The root mean square error (RMSE) ranges from $33$ W m$^{-2}$ (5 \%) to $64$ W m$^{-2}$ (10 \%). The correlation coefficient ranges between 0.84 and 0.98. This work demonstrates the quality of the McClear model combined with MACC products, and indirectly the quality of the aerosol properties modelled by the MACC reanalysis.

1 Introduction

The downwelling solar irradiance observed at ground level on horizontal surfaces and integrated over the whole spectrum (total irradiance) is called surface solar irradiance (SSI). It is the sum of the direct irradiance, from the direction of the sun, and the diffuse, from the rest of the sky vault, and is also called the global irradiance. The SSI is an essential climate variable (ECV) as established by the Global Climate Observing System in August 2010 (GCOS, 2012). Knowledge of the SSI and its geographical distribution is of prime importance for numerous domains where SSI plays a major role as e.g. weather, climate, biomass, and energy.

Accurate assessments of SSI can be retrieved from satellite data, and several studies demonstrate the superiority of satellite data over interpolation methods applied to sparse measurements performed within a radiometric network (Perez et al., 1997; Zelenka et al., 1999). Given the scarcity of long-term SSI measurements made at ground level, several authors mention that satellite-derived SSI may supplement these measurements (Ba et al., 2001; Blanc et al., 2010; Cano et al., 1986; Darnell et al., 1996; Diabaté et al., 1988; Elias and Roujean, 2008; Lefèvre et al., 2007; Posselt et al., 2012; Raschke et al., 1987; Schiffer and Rossow, 1985; Schmetz, 1989).

Hereafter, a model estimating the SSI under clear sky is called a clear-sky model. As it describes the SSI in a cloud-free atmosphere, it estimates a realistic upper limit of the
SSI (Gueymard, 2012; Long and Ackerman, 2000). In many methods for the assessment of the SSI, all-sky irradiance is derived from the modelled clear-sky SSI by the attenuation or a modification factor due to clouds (Cano et al., 1986; Posselt et al., 2012; Raschke et al., 1987; Rigollier et al., 2004). While the all-sky SSI changes mainly with clouds, the SSI under clear sky is strongly dependent on the composition of the atmosphere, namely the variable parameters aerosol and water vapour. Aerosols play a major role due to the diversity in scattering and absorbing properties according to their type, and the spatial and temporal heterogeneity of their number, size, chemical composition, and shape (Deepshikha et al., 2006; Deneke et al., 2008; Elias and Roujean, 2008; Gueymard, 2005; Xu et al., 2011).

The MACC project (Monitoring Atmosphere Composition and Climate), funded by the European Commission, is preparing the operational provision of global aerosol property forecasts together with physically consistent total column content in water vapour and ozone (Kaiser et al., 2012a; Peuch et al., 2009). Up to now a multi-annual reanalysis data set is provided and used here (Inness et al., 2013). Such information has not been available so far from any operational numerical weather prediction (NWP) centre.

A new clear-sky model called McClear has been developed to exploit this new input data source for estimating the downwelling shortwave direct and global irradiances received at ground level. The aim of this article is to describe this model (Sect. 2) and its implementation (Sect. 3), and to establish its performance (Sects. 4 to 6) with respect to this model (Sect. 2) and its implementation (Sect. 3), and the available high-quality measurements of SSI and the existing literature (Sect. 7).

2 The McClear model

Let $E^\text{diff}$ denote the diffuse irradiance on the horizontal plane, $E^\text{dir}$ the direct (or beam) irradiance on the horizontal plane, and $E^\text{glo}$ the global irradiance:

$$E^\text{glo} = E^\text{diff} + E^\text{dir}. \quad (1)$$

If $E_0$ denotes the irradiance that is received on a horizontal surface at the top of the atmosphere for the location and time under consideration, the clearness index KT is defined as

$$\text{KT} = \frac{E^\text{glo}}{E_0}. \quad (2)$$

The clearness index is also called global transmissivity of the atmosphere, or atmospheric transmittance, or atmospheric transmission. In the same way, we define the direct clearness index $\text{KT}^\text{dir}$ as

$$\text{KT}^\text{dir} = \frac{E^\text{dir}}{E_0}. \quad (3)$$

The model McClear aims at producing both $E^\text{glo}$ and $E^\text{dir}$. The first constraint put in its development is that it should sufficiently accurately reproduce the SSI estimated by accurate radiative transfer models (RTM). The RTM libRadtran (Mayer and Kylling, 2005; Mayer et al., 2010) is taken here as a reference. The deviations between McClear and libRadtran outputs must obey constraints similar to those for radiation measurements (WMO, 2008): the bias shall be less than 3 W m$^{-2}$, and 95% of the differences should be less than 20 W m$^{-2}$.

The major constraint is that it should deliver time series of irradiance much faster than libRadtran. The computational speed should be approximately $10^5$ times greater in order to enable routine production in real-time forecasting systems.

One solution to obey these constraints is to adopt the abaci approach combined with interpolation functions. The use of abaci – also known as look-up tables (LUT) – is not new in this domain (Deneke et al., 2008; Huang et al., 2011; Mueller et al., 2009; Schulz et al., 2009). It reveals an efficient and fast means to provide estimates of values otherwise available from complex and slow models. One drawback is the resources and time needed to compute the abaci that may amount to months. Another drawback is that the abaci formulation has to be adapted to the available input data source. Therefore, this paper deals with the specifics of an abaci approach for typical numerical weather prediction output characteristics as represented in the MACC reanalysis data set.

A set of abaci and interpolation functions to speed up the solution of the radiative transfer equations is designed, developed and implemented. This ensemble of abaci and interpolation functions as well as functions to exploit them for aggregation in time and computation of the sum position is the model McClear.

Inputs to McClear are the solar zenith angle, the ground albedo and 6 parameters describing the optical state of the atmosphere:

- total column content of ozone and water vapour,
- vertical profile of temperature, pressure, density, and volume mixing ratio for gases as a function of altitude taken in the AFGL data sets (see Sect. 3.2),
- aerosol optical depth (AOD) at 550 nm, Ångström coefficient, and aerosol type: urban, continental clean, continental polluted, continental average, maritime clean, maritime polluted, maritime tropical, Antarctic, and desert (see Sect. 3.4),

and other parameters describing the geographical location and the time:

- latitude, longitude and elevation above mean sea level (a.s.l.) of the site of interest,
- period of time requested,
- integration period, also known as the summarization period, of the radiation: 1 min, 15 min, 1 h, and 1 day,
– and time sampling step, usually identical to the integration period.

Aerosols are described by standard aerosol types instead of using modelled AOD at different wavelengths explicitly. At the first glance this can be criticized as making no use of available additional aerosol type information and it creates the need of a transition matrix from MACC output to aerosol type (see Sect. 3.4). However, it enhances the flexibility of the McClear use for other future sources of input data using other internal aerosol models and/or other output wavelengths. Additionally, it avoids the increase of the abacis in order to cover all AOD wavelengths and the shift for spectral interpolation assumptions from the AOD level on the irradiance level afterwards in the broadband irradiance generation.

The abacis contain

– the clearness index $K_T$ for ground albedo equal to 0, 0.1, and 0.9 (see Sect. 3.1),
– the direct clearness index $K_{T_{dir}}$ for null ground albedo,

for selected values of the 10 following parameters:

– solar zenith angle $\theta_S$,
– ground albedo,
– the altitude of the ground level and elevation above the ground,
– and the 6 parameters describing the optical state of the clear atmosphere and already listed above.

These values are called node points. The clearness indices are obtained by running libRadtran for these node points. Interpolation functions permit to interpolate between node points.

Altitude of the ground level and elevation above the ground are both needed because the 6 clear-sky parameters are computed in the MACC analysis for a very smooth terrain and therefore represent the atmospheric properties for this atmospheric column. The altitude of this smooth terrain model may differ from the elevation of the more local site of interest and the SSI should be corrected, assuming that the difference in SSI between the local elevation and the smooth terrain is equivalent to the difference in SSI between a similar elevation above ground level, i.e. in the atmosphere, and the smooth terrain. The correction is explained in Sect. 3.3.

An optimization was made for the selection of the node points and interpolation functions with the following constraints: (i) minimize the number of node points in order to have abaci as small as possible, (ii) select/design interpolation/extrapolation functions as fast as possible, and (iii) interpolated values must be close to the libRadtran results with already mentioned constraints. The last constraints on the difference with libRadtran were checked for each input separately as well as the combination of all inputs using all node points and interpolation functions.

The optimization was done for each of the 10 inputs listed above. A Monte Carlo technique is applied to randomly generate sets of inputs to libRadtran within the 10-D space, with the exception of the current parameter which is regularly sampled with a small step. The optical properties were selected by considering their observed marginal distribution. More precisely, the uniform distribution is chosen as a model for marginal probability for all parameters except aerosol optical thickness, Ångström coefficient, and total column ozone. The chi-square law for aerosol optical thickness, the normal law for the Ångström coefficient, and the beta law for total column ozone have been selected. The parameters of the laws are empirically determined from the analyses of the observations made in the AERONET network for aerosol properties and from meteorological satellite-based ozone products.

For all inputs, the selected interpolation/extrapolation functions are linear interpolators/extrapolators, except for the solar zenith angle $\theta_S$. For the latter, the modified Beer–Lambert (MLB) function proposed by Mueller et al. (2009) has been studied. To obey the constraints, a 5-piecewise MLB was retained with the following angles: 0°, 60°, 75°, 80°, 85°, and 89.9° instead of the originally proposed two angles 0° and 60°. Shortly after the design of the abaci was frozen, Qu et al. (2011) demonstrated that a 4-piecewise MLB with the angles 0°, 60°, 75°, 85°, and 89.9° would have been applicable as well.

Following Oumbe et al. (2011), the efficiency and accuracy of piecewise linear functions to estimate changes in $E^{\text{blo}}$ and $E_{\text{dir}}$ with altitude above the ground is sufficient.

The formula of Vermote et al. (1994, 1997),

$$ K_T(\rho_g) = K_T(\rho_g = 0)/(1 - \rho_g S), $$

(4)

describes the change in $K_T$ as a function of the ground albedo $\rho_g$ and the atmospheric spherical albedo $S$. $\rho_g$ is an input while $S$ is unknown. In principle, $S$ can be computed knowing $K_T$ for any value of $\rho_g$ using Eq. (4). In practice, better results are attained if $S$ is computed for two values of $\rho_g = 0.1$, and 0.9 using Eq. (4) – and then is linearly interpolated/extrapolated for the actual $\rho_g$:

$$ a = [S(\rho_g = 0.9) - S(\rho_g = 0.1)]/0.8 $$

(5)

$$ b = S(\rho_g = 0.1) - 0.1a $$

$$ S = a\rho_g + b. $$

In total, this design results in 1674 abaci. One abacus corresponds to a given atmospheric profile and a given type of aerosol. In an abacus, the list of node points is as follows:

– total column content in ozone (in Dobson unit): 200, 300, 400, 500,
– total column content in water vapour (kg m$^{-2}$): 0.1, 3, 5, 7, 10, 15, 20, 30, 40, 60, 80, and 100,
aerosol optical depth at 550 nm: 0.01, 0.05, 0.1, 0.2, 0.3, 0.5, 1, 1.5, 2, and 5,
aerosol Ångström coefficient: -1, -0.5, 0, 0.5, 1, 1.5, 2, 3, and 4,
site elevation above mean sea level (km): 0, 1, 2, 3, 4, 5, 6, and 7,
elevation above ground level (km): 0, 0.5, 1, 1.5, and 2,
solar zenith angle (deg): 0, 60, 75, 80, 85, and 89.9.

3 Practical implementation of McClear

McClear can be run with self-defined inputs. More interestingly, it is capable of ingesting atmospheric data from the MACC modelling and from the MODIS (Moderate Resolution Imaging Spectroradiometer) estimates for ground albedo. This section details the practical implementation of McClear.

3.1 Ground albedo

The MCD43C1 and MCD43C2 data, derived from MODIS images, are 16-day composites provided as a level-3 product projected to a 0.05° grid in latitude/longitude. They are produced every 8 days with 16 days of acquisition, where the given date is that of the first day of the 16-day period. These data sets contain three model parameters, called fiso, fvol, and fgeo (Schaaf et al., 2002). fiso describes the isotropic part of the BRDF; the two other parameters are linked to the viewing and illuminating geometry to describe the anisotropic part of the BRDF. The directional hemispherical reflectance (DHR) – also known as black-sky albedo – and the bihemispherical reflectance (BHR) – also known as white-sky albedo – (e.g. Schaepman-Strub et al., 2006) are computed from the BRDF using formulas in Schaaf et al. (2002). Defining \( K_{\text{dir}}(\rho_g) \) as

\[
K_{\text{dir}}(\rho_g) = E_{\text{dir}}/E_{\text{ghi}}(\rho_g)
\]

where \( E_{\text{dir}} \) does not depend on \( \rho_g \), the ground albedo \( \rho_g \) is given by

\[
\rho_g = \text{BHR} + K_{\text{dir}}(\rho_g)(\text{DHR} - \text{BHR}).
\]

The major difficulty in Eq. (7) is that \( \rho_g \) depends upon \( K_{\text{dir}} \), which depends itself on \( \rho_g \). By combining Eqs. (4)–(7), and denoting \( \Delta = (\text{DHR} - \text{BHR}) \), one obtains a second-order equation in \( KT \) which is the quantity of interest:

\[
a \Delta^2 K T^2 + 2 a \Delta K T + \Delta K T^2 = 0.
\]

Using the Monte Carlo technique to randomly select 100,000 samples, it is found that Eq. (8) has only one solution that respects \( KT > KT_{\text{dir}} \). Therefore, Eq. (8) is used to compute \( KT \) and Eq. (7) provides \( \rho_g \).

In a practical manner, once a request is made for a given site, the three BRDF parameters fiso, fvol, and fgeo are taken from the closest MCD43C1 or MCD43C2 grid point. Then, Eq. (8) is solved for \( KT \) for each minute of the day.

The difference between the MCD43C1 and MCD43C2 products is that MCD43C2 is a snow-free version of MCD43C1. Both products exhibit gaps in time and space. Two approaches have been tested to palliate the lack of data.

In the first approach, the three BRDF parameters were taken from the MCD43C2 product for the previous, current and following months for the current day. They were interpolated in time for each minute of the day, taking into account the possible absence of data. Sometimes, data may not be available for three months in a row. In these cases, the parameters were replaced by their mean values computed for the given month over the period 2004–2011. Over the ocean, fiso was set to 0.02 (Wald and Monget, 1983) and the two parameters to 0. Several gaps in space and time were still observed. Presence of snow is not accounted for, and this may induce errors in the diffuse irradiance in some cases.

The second approach consisted in computing mean values of the three BRDF parameters from the MCD43C1 product for each of the twelve months of the year over the period 2004–2011. Each mean value was allotted to the mid-day of each month. The values for the current day were computed by linear interpolation using the current month and that before or after depending on the case. A great deal of effort has been made on the completion of data which are missing mostly in water-covered areas. The “Land Cover Type” product is also a MODIS product using the same grid as MCD43C1. It allows the identification of pixels containing water and the proportion of water in this pixel. Let \( W \) denote the binary mask for water; \( W = 1 \) if the pixel has been classified as “water” at least once for the given month during the period 2001–2009 covered by the “Land Cover Type” product, and is 0 otherwise. Let \( P \) be the average proportion of the water. The typical triplet \( f_w = (\text{fiso}, \text{fvol}, \text{fgeo}) \) for water areas was defined by the mode of the valid triplets \( (\text{fiso}, \text{fvol}, \text{fgeo}) \) for water pixels comprised between latitude \(-45^\circ\) and latitude \(45^\circ\). \( f_w \) was allotted to each unknown water pixel for which \( P = 1 \). Then, if a water pixel exhibited a valid triplet \( f \) and a proportion of water \( P \) less than 1, \( f \) was replaced by a linear combination \( f_w = f + (1 - P) f_w \). A moving average of ±1 month was applied followed by a median filter of 11 × 11 pixels to fill gaps. This two-step filtering was repeated but with a window of ±2 months. Then, a median filter of 21 × 21 pixels was applied. Still unknown were a few pixels in the middle of the ocean, extreme southern part of the Antarctic Ocean, and Greenland. They were treated manually and were allotted the mean value of the triplets \( f \) averaged in their neighbourhood.

When compared to ground-based measurements of the SSI as discussed later, both approaches gave the same results with very small differences not taking into account the gaps. The
second approach is used in the following. It has the advantage that it makes easier the implementation of McClear.

3.2 Atmospheric profile

The five vertical profiles of temperature, pressure, density, and volume mixing ratio for gases as a function of altitude used in McClear are those from the USA Air Force Geophysics Laboratory (AFGL) as implemented in libRadtran: tropics, mid-latitude summer and winter, and sub-Arctic summer and winter. A mask has been constructed for the automatic selection of the atmospheric profile for any site. The Köppen climate classification map (FAO, 1997) has been manually modified for North America, China and Africa following Trewartha (1954). Other maps of climate classification could have been suitable and possibly more accurate. But aiming at partitioning the world into five classes only, a very limited level of detail is sufficient. The sub-Arctic profiles are allotted to climate zones noted EF, ET, DC, DD in Trewartha (1954), the tropical profile to Aw, As, Af, and Am, and the mid-latitude profiles are allotted to the rest. Oceans are not covered by these climate maps; extension was manually made. As for the seasons, November to April is considered as boreal winter (auroral summer).

3.3 Altitude correction

The 6 inputs from MACC are given for grid nodes, which are separated by approximately 100 km. A very smooth elevation model is used in MACC analyses, and each node has a known local mean elevation above mean sea level (a.s.l.). The MACC-equivalent elevation for the local site under consideration is computed by linear interpolation of the MACC elevations of the 4 neighbouring grid nodes. Then, interpolation in the clearness index is made for this MACC-equivalent elevation using the two closest nodes “site elevation” in the abaci. If the actual elevation of the local site is less than the MACC-equivalent elevation, the clearness index is set to that corresponding to the MACC-equivalent elevation. Otherwise, an additional linear interpolation/extrapolation is performed using the nodes “elevation above ground level”.

3.4 Aerosols properties

Inputs to McClear are the aerosol optical depth at 550 nm, Ångström coefficient, and aerosol type. The MACC reanalysis delivers total aerosol optical depth at 550 and 1240 nm, from which the Ångström coefficient is derived. It delivers also partial optical depths at 550 nm for dust, organic, sea salt, sulphate, and black carbon aerosol species (Benedetti et al., 2009; Kaiser et al., 2012b; Morcrette et al., 2008, 2009).

These partial optical depths are used to automatically determine the aerosol type, and more exactly the mixture whose name describes the typical origin of the particle ensembles: urban, continental clean, continental polluted, continental average, maritime clean, maritime polluted, maritime tropical, Antarctic, and desert. Table 1 in Holzer-Popp et al. (2002) gives percentage contributions to the total optical depth of the respective mixtures by the basic components: water soluble, water insoluble, sea salt accumulation mode, coarse mode, soot, and mineral transported. It is used as a guide for converting MACC species into types. The partial optical depths are converted to fractions of the total optical depth, in percent. The conversion algorithm is described in Fig. 1. The type “Antarctic” is solely defined by the latitude.

The algorithm has been tested by running it over several years of MACC data. Several sites were selected for which one or more types were expected to dominate, such as sites in the Indian and South Pacific oceans (marine tropical and maritime clean and polluted), North Atlantic Ocean (marine, continental, and urban), Australian and Sahelian deserts (desert and continental), Tibetan Plateau and Amazonian forest (mostly continental and maritime), Zaire forest (continental and urban), and large conurbations: Calcutta and New Delhi (urban and continental polluted), Beijing (urban), Shanghai and Mexico (urban, continental, and maritime), Tamanrasset, Sede Boqer, and Mezaira (desert).

For each site, the histogram of the resulting types has been drawn and checked that it was close to our expectations. Though satisfactory as a whole, more work is needed on this algorithm, which may fail sometimes. Figure 2 exhibits \(E^{\text{glo}}\) measured at the station Carpentras every 1 min on 10 June 2006 and that estimated by McClear as an example of such a failure. This day was clear, except in the early morning before 07:00 UTC. One can see that both curves agree perfectly; the aerosol type was found as “urban”. There is an exception to the agreement from 08:00 to 11:30 UTC where the type was found as “marine polluted”. This leads to an overestimation of \(E^{\text{glo}}\) with a peak of 30 W m\(^{-2}\) from 998 W m\(^{-2}\) down to 968 W m\(^{-2}\), i.e. 3% of \(E^{\text{glo}}\) at 11:30 UTC. At this instant, \(E^{\text{dir}}\) amounts to 910 W m\(^{-2}\) and is unchanged as it does not depend upon the aerosol type.

3.5 Computing instantaneous clear-sky SSI for any site

Aerosol properties, and total column contents of water vapour and ozone in MACC are given every 3 h, starting at 00:00 UT. A bi-linear interpolation in space is applied to compute a time series of 3 h values for the given location. A further interpolation in time is performed yielding time series of these atmospheric quantities every 1 min in order to enable the production of 1 and 15 min SSI.

These 1 min values are inputs to the McClear model. The solar zenith angle is computed with the SG2 algorithm (Blanc and Wald, 2012) for the middle of the minute. An abacus is selected for the given atmospheric profile and aerosol type. A series of interpolations as described above is performed to yield the clearness indices. The ordering of interpolation of parameters was found as having a negligible influence on the results. For the sake of computing speed,
linear interpolations are performed first, then the MLB interpolator, and finally the computation of the ground albedo.

The resulting clearness indices are assumed to be constant over 1 min. The 1 min mean irradiance is computed by Eqs. (2)–(3), where the solar geometry parameters and \( E_0 \) are determined by SG2 for the beginning and end of the minute. If requested, the 1 min irradiances are summarized to yield 15 min, hourly and daily values in Universal Time or True Solar Time.

Various tests have been made for comparing outputs from McClear and libRadtran to check that both models yield similar results. Several tests have been made with a random selection of inputs and were satisfactory. The targets were met: the bias was less than 3 W m\(^{-2}\) and 95 % of the differences were less than 20 W m\(^{-2}\).

### 4 BSRN data for validation

The Baseline Surface Radiation Network (BSRN) is a collection of measurements of \( E^{\text{glo}} \), \( E^\text{diff} \) and beam normal irradiance (BNI) of high quality suitable for validation. Measurements are acquired every 1 min. Uncertainty requirements for BSRN data are 5 W m\(^{-2}\) for global irradiance and 2 W m\(^{-2}\) for direct irradiance (Ohmura et al., 1998). Data sets were collected for 11 stations representing a variety of climates (Table 1) for the period 2005–2008, except for Palaiseau, Xianghe and Lauder (2005–2007) and Brasilia (2006–2007).

Following the recommendations of Roesch et al. (2011), only the BSRN measurements were kept which obey the following constraints:

\[
\text{if } \theta_s \leq 75^\circ, \quad 1.08 \geq (E^\text{diff} + E^\text{dir})/E^{\text{glo}} \geq 0.92
\]

\[
\text{if } \theta_s > 75^\circ, \quad 1.15 \geq (E^\text{diff} + E^\text{dir})/E^{\text{glo}} \geq 0.85.
\]

Roesch et al. (2011) note a percentage of missing data of 4 % for global irradiance and 13 % for direct irradiance for all studied BSRN data.

Two filters have been applied on the remaining BSRN data in order to retain reliable clear-sky instants. The first one was a constraint on the amount of diffuse irradiance with respect to the global irradiance since the direct irradiance is prominent in the case of clear sky. Only those minutes for which \( E^\text{diff} / E^{\text{glo}} < 0.3 \), i.e. when the diffuse component is much less than the direct one, have been retained.

The second filter dealt with the temporal variability of the irradiance. If there is no cloud, the sky should be clear for a long period. Checking this would avoid cases of broken clouds or noticeable spatial heterogeneity around the site if ergodicity is assumed. The first step of this filter was to retain

![Fig. 1. Sketch of the algorithm converting the total optical depth (AOD) and partial optical depths of MACC species – dust (AODdu), sea salt (AODss), black carbon (AODbc), and organic matter (AODor) – into aerosol types: urban, continental clean, continental polluted, continental average, maritime clean, maritime polluted, maritime tropical, Antarctic, and desert. “lat” is latitude.](image-url)
only periods with enough measurements that have passed the first filter. A given instant \( t \), expressed in min, was kept only if at least 30% of the 1 min observations in both intervals \([t - 90, t]\) and \([t, t + 90]\) have been retained after the first filter. A corrected clearness index, \( \text{KT}' \) (Ineichen and Perez, 1999) is computed for this instant:

\[
\text{KT}' = \frac{\text{KT}}{[1.031 \exp(-1.4/((0.9 + 9.4/m))) + 0.1]},
\]

where \( m \) is the air mass defined by Kasten and Young (1989):

\[
m(\Theta_S) = \frac{(p/p_0)}{[\cos(\Theta_S) + 0.50572(\Theta_S + 6.07995)^{-1.6364}],}
\]

where \( \Theta_S \) is expressed in degree, and \( p \) and \( p_0 \) are respectively the pressure at the site under consideration and that at sea level.

An instant was considered clear if the standard deviation of \( \text{KT}' \) in the interval \([t - 90, t + 90]\) was less than a threshold, set empirically to 0.02. Only these 1 min clear-sky instants were retained for the validation. Figure 3 displays a time series of \( E_{\text{glo}} \) for the selected clear-sky instants in the year 2005 in Payerne, in black circles. Payerne experiences a large number of clear skies during the year and many instants are selected. In this graph are also drawn the clear-sky instants selected by the algorithm of Long and Ackerman (2000), in light-grey crosses. One may see that they are differences between the results. The proposed algorithm presents less low values of \( E_{\text{glo}} \) than that of Long and Ackerman and offers more confidence in the fact that the instant is clear.

5 Validation using BSRN data

The validation of McClear was made by comparing the aforementioned 1 min BSRN values for clear sky and the McClear values calculated for these instants and the location of the site. Following the ISO standard (1995), the deviations were computed by subtracting measurements for each instant from the McClear estimations, and they were summarized by the bias, the root mean square error (RMSE), and the squared correlation coefficient. The parameters of the least-squares fitting line were also computed. Relative values are expressed with respect to the mean observed value. This operation has been performed for \( E_{\text{glo}} \) and \( E_{\text{dir}} \), \( \text{KT} \) and \( \text{KT}' \), site per site, with all instants merged, and for different classes of \( E_{\text{glo}} \), \( E_{\text{dir}} \), \( \text{KT} \), \( \text{KT}' \), \( \Theta_S \), aerosol optical depth at 550 nm, aerosol Ångström coefficient, aerosol type, atmospheric profile, total content in water vapour and ozone, ground albedo, year and month.

Figures 4 and 5 are scatter density plots between measured and estimated \( E_{\text{glo}} \) and \( E_{\text{dir}} \) for Payerne. An overall good fit is observed between estimates and observations: the points are well aligned along the 1:1 line with a small tendency towards overestimation with high \( E_{\text{glo}} \) and a limited scattering. The squared correlation coefficients are very large: 0.99 and 0.96 respectively, meaning that 99% and 96% of information contained in \( E_{\text{glo}} \) and \( E_{\text{dir}} \) is well explained by McClear. The relative bias is small − 4% for \( E_{\text{glo}} \) and 1% for \( E_{\text{dir}} \) − as is the RMSE: 5% and 7%. As expected, performances in \( E_{\text{dir}} \) are less than for \( E_{\text{glo}} \); the effects of aerosols are more pronounced in beam than in global SSI. Cases of

---

Table 1. List of BSRN stations used for validation.

<table>
<thead>
<tr>
<th>Station</th>
<th>Code</th>
<th>Country</th>
<th>Latitude</th>
<th>Longitude</th>
<th>Elevation a.s.l. (m)</th>
<th>MACC mean altitude (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Barrow</td>
<td>BAR</td>
<td>USA (Alaska)</td>
<td>71.323</td>
<td>-156.607</td>
<td>8</td>
<td>31</td>
</tr>
<tr>
<td>Palaiseau</td>
<td>PAL</td>
<td>France</td>
<td>48.713</td>
<td>2.208</td>
<td>156</td>
<td>126</td>
</tr>
<tr>
<td>Carpentras</td>
<td>CAR</td>
<td>France</td>
<td>44.083</td>
<td>5.059</td>
<td>100</td>
<td>538</td>
</tr>
<tr>
<td>Payerne</td>
<td>PAY</td>
<td>Switzerland</td>
<td>46.815</td>
<td>6.944</td>
<td>491</td>
<td>943</td>
</tr>
<tr>
<td>Xianghe</td>
<td>XIA</td>
<td>China</td>
<td>39.754</td>
<td>116.962</td>
<td>32</td>
<td>326</td>
</tr>
<tr>
<td>Tateno</td>
<td>TAT</td>
<td>Japan</td>
<td>36.050</td>
<td>140.133</td>
<td>25</td>
<td>246</td>
</tr>
<tr>
<td>Sede Boqer</td>
<td>SBO</td>
<td>Israel</td>
<td>30.905</td>
<td>34.782</td>
<td>500</td>
<td>450</td>
</tr>
<tr>
<td>Tamanrasset</td>
<td>TAM</td>
<td>Algeria</td>
<td>22.780</td>
<td>5.510</td>
<td>1385</td>
<td>1012</td>
</tr>
<tr>
<td>Brasilia</td>
<td>BRB</td>
<td>Brazil</td>
<td>-15.601</td>
<td>-47.713</td>
<td>1023</td>
<td>808</td>
</tr>
<tr>
<td>Alice Springs</td>
<td>ASP</td>
<td>Australia</td>
<td>-23.798</td>
<td>133.888</td>
<td>547</td>
<td>554</td>
</tr>
<tr>
<td>Launder</td>
<td>LAU</td>
<td>New Zealand</td>
<td>-45.045</td>
<td>+169.689</td>
<td>350</td>
<td>509</td>
</tr>
</tbody>
</table>
large deviations can be related to errors in estimation of the aerosol optical thickness. As a whole, there is a slight overestimation by McClear for both $E_{\text{glo}}$ and $E_{\text{dir}}$. The bias and RMSE exhibit a tendency to decrease with increasing $\Theta_1$. This will be discussed later. Aerosol types are mostly “maritime polluted” by far, then “urban”, then “continental polluted”; the aerosol optical depth at 550 nm is mostly found between 0.01 and 0.30. No trend is observed in bias and RMSE as a function of these properties.

Figures 6 and 7 are scatter density plots between BSRN data and McClear estimates for the global and beam clearness indices. The changes in solar radiation at the top of the atmosphere due to changes in geometry, namely the daily course of the sun and seasonal effects, are usually well reproduced by models and lead to a de facto correlation between observations and estimates of SSI hiding potential weaknesses. Clearness indices KT and KT\textsuperscript{dir} are stricter indicators of the performances of a model regarding its ability to estimate the optical state of the atmosphere. Though KT and KT\textsuperscript{dir} are not completely independent of $\Theta_S$ as they decrease as $\Theta_S$ increases, the dependency is much less pronounced than in SSI. In Figs. 6 and 7, KT and KT\textsuperscript{dir} exhibit a lower squared correlation coefficient than $E_{\text{glo}}$ and $E_{\text{dir}}$: 0.69 and
0.53, instead of 0.99 and 0.96. These low correlation coefficients are explained by the limited range of values taken by these indices because only clear sky is dealt with and do not necessarily imply poor performance. In both figures, the set of points is well aligned along the 1:1 line with a slight overestimation for KT and no bias for KTdir. The relative bias and RMSE for KT are 3% and 5%, similar to those for Eglo. The relative bias and RMSE for KTdir are small: 1% and 8%, very similar to those for Edir.

Figures 8 to 11 are scatter density plots between BSRN data and McClear estimates for respectively Eglo, Edir, KT, and KTdir for Xianghe. Xianghe is a rural city but under the influence of the air pollution in Beijing (Wang et al., 2011). It is also the seat of an AERONET station, which shows that the fine mode is very often encountered. An overall good fit is observed between estimates and observations for both Eglo and Edir. The relative bias is small – −1% for Eglo and −3% for Edir – as is the RMSE: 5% and 10%. The squared correlation coefficients are large for the global (0.91) but low for the direct (0.74), meaning that 91% and 74% of information contained in Eglo and Edir is well explained by McClear. Aerosol types estimated by McClear are mostly “urban” by far, then “desert” and then “continental polluted” in
agreement with AERONET observations. Wang et al. (2011) found that the aerosol optical depth estimated by MODIS and further assimilated in the MACC analyses is greater than that observed by the AERONET instrument. This may explain the underestimation of $E_{\text{glo}}$ by McClear. The range of values for $E_{\text{dir}}$ is also very large ($\geq 0.95$) for all stations (Table 2). The bias ranges between $-7$ and $+25 \text{ W m}^{-2}$, i.e. less than $4\%$ of the mean observed value. Largest biases in relative value are found in Brasilia (Brazil), Payerne (Switzerland), and Carpentras (France). The slope of the fitting line is close to 1, between 0.96 and 1.04. The RMSE ranges between 20 and 36 $\text{ W m}^{-2}$ and is less than $5\%$ of the mean observed value in all cases.

One should note that the statistical quantities slightly vary from one year to another. For example, the bias in $E_{\text{glo}}$ for Payerne is $23 \text{ W m}^{-2}$ in 2005, $17 \text{ W m}^{-2}$ in 2006, $23 \text{ W m}^{-2}$ in 2007, and $26 \text{ W m}^{-2}$ in 2008. As a whole, no clear trend was observed between these quantities and the year. There is also no clear trend with the aerosol properties and type, ground albedo, or content in ozone and water vapour. However, it appears that results are usually better for the summer months than for winter. The bias varies with $\Theta_S$ though no trend appears (Fig. 12). The RMSE exhibits a tendency to decrease with increasing $\Theta_S$, but one should note that the changes may be complex (Fig. 13). The relative bias and the relative RMSE are not constant as a function of $\Theta_S$.

The correlation coefficient for $E_{\text{dir}}$ (Table 3) is also very large ($r \geq 0.96$) for all stations except Xianghe ($r = 0.86$). The bias ranges between $-48$ and $+33 \text{ W m}^{-2}$, and is less than $7\%$ of the mean observed value. Lowest biases in absolute values, less than $6 \text{ W m}^{-2}$, are found in

### Table 2. Comparison between clear-sky global irradiances measured by BSRN and estimated by McClear.

<table>
<thead>
<tr>
<th>Station</th>
<th>Number of samples</th>
<th>Mean observed value $\text{ W m}^{-2}$</th>
<th>Bias $\text{ W m}^{-2}$</th>
<th>Rel. bias %</th>
<th>RMSE $\text{ W m}^{-2}$</th>
<th>Fitted straight line</th>
<th>Squared correl. coeff.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Barrow</td>
<td>70283</td>
<td>498</td>
<td>$-6$</td>
<td>$-1%$</td>
<td>21</td>
<td>4%</td>
<td>0.96$x+14$</td>
</tr>
<tr>
<td>Palaiseau</td>
<td>29222</td>
<td>598</td>
<td>7</td>
<td>1%</td>
<td>25</td>
<td>4%</td>
<td>1.03$x-8$</td>
</tr>
<tr>
<td>Carpentras</td>
<td>300468</td>
<td>596</td>
<td>$+20$</td>
<td>$+3%$</td>
<td>29</td>
<td>5%</td>
<td>1.04$x-1$</td>
</tr>
<tr>
<td>Payerne</td>
<td>136879</td>
<td>629</td>
<td>$+22$</td>
<td>$+4%$</td>
<td>31</td>
<td>5%</td>
<td>1.02$x+10$</td>
</tr>
<tr>
<td>Xianghe</td>
<td>33795</td>
<td>791</td>
<td>$-7$</td>
<td>$-1%$</td>
<td>36</td>
<td>5%</td>
<td>0.98$x+8$</td>
</tr>
<tr>
<td>Tateno</td>
<td>133433</td>
<td>590</td>
<td>$+10$</td>
<td>$+2%$</td>
<td>29</td>
<td>5%</td>
<td>1.01$x+3$</td>
</tr>
<tr>
<td>Sede Boqer</td>
<td>304550</td>
<td>785</td>
<td>$+12$</td>
<td>$+2%$</td>
<td>27</td>
<td>4%</td>
<td>0.96$x+40$</td>
</tr>
<tr>
<td>Tamanrasset</td>
<td>331045</td>
<td>791</td>
<td>$+8$</td>
<td>$+1%$</td>
<td>20</td>
<td>3%</td>
<td>0.96$x+38$</td>
</tr>
<tr>
<td>Brasilia</td>
<td>73563</td>
<td>649</td>
<td>$+25$</td>
<td>$+4%$</td>
<td>35</td>
<td>5%</td>
<td>1.02$x+13$</td>
</tr>
<tr>
<td>Alice Springs</td>
<td>442315</td>
<td>715</td>
<td>$+11$</td>
<td>$+2%$</td>
<td>23</td>
<td>3%</td>
<td>1.00$x+12$</td>
</tr>
<tr>
<td>Lauder</td>
<td>117090</td>
<td>600</td>
<td>$+6$</td>
<td>$+1%$</td>
<td>21</td>
<td>4%</td>
<td>0.99$x+13$</td>
</tr>
</tbody>
</table>

### Table 3. Comparison between clear-sky beam irradiances on horizontal surface measured by BSRN and estimated by McClear.

<table>
<thead>
<tr>
<th>Station</th>
<th>Number of samples</th>
<th>Mean observed value $\text{ W m}^{-2}$</th>
<th>Bias $\text{ W m}^{-2}$</th>
<th>Rel. bias %</th>
<th>RMSE $\text{ W m}^{-2}$</th>
<th>Fitted straight line</th>
<th>Squared correl. coeff.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Barrow</td>
<td>70283</td>
<td>406</td>
<td>$-21$</td>
<td>$-5%$</td>
<td>41</td>
<td>10%</td>
<td>0.96$x-3$</td>
</tr>
<tr>
<td>Palaiseau</td>
<td>29222</td>
<td>492</td>
<td>$-3$</td>
<td>$-1%$</td>
<td>37</td>
<td>7%</td>
<td>1.02$x-13$</td>
</tr>
<tr>
<td>Carpentras</td>
<td>300468</td>
<td>505</td>
<td>$-1$</td>
<td>$-0%$</td>
<td>35</td>
<td>7%</td>
<td>1.00$x-2$</td>
</tr>
<tr>
<td>Payerne</td>
<td>136879</td>
<td>530</td>
<td>$+6$</td>
<td>$+1%$</td>
<td>39</td>
<td>7%</td>
<td>0.99$x+14$</td>
</tr>
<tr>
<td>Xianghe</td>
<td>33795</td>
<td>642</td>
<td>$-22$</td>
<td>$-4%$</td>
<td>64</td>
<td>11%</td>
<td>0.86$x+66$</td>
</tr>
<tr>
<td>Tateno</td>
<td>133433</td>
<td>485</td>
<td>$-16$</td>
<td>$-3%$</td>
<td>44</td>
<td>9%</td>
<td>1.04$x-37$</td>
</tr>
<tr>
<td>Sede Boqer</td>
<td>304550</td>
<td>667</td>
<td>$-48$</td>
<td>$-7%$</td>
<td>62</td>
<td>9%</td>
<td>0.98$x-38$</td>
</tr>
<tr>
<td>Tamanrasset</td>
<td>331045</td>
<td>653</td>
<td>$+16$</td>
<td>$+2%$</td>
<td>48</td>
<td>7%</td>
<td>1.05$x-14$</td>
</tr>
<tr>
<td>Brasilia</td>
<td>73563</td>
<td>560</td>
<td>$+33$</td>
<td>$+6%$</td>
<td>48</td>
<td>9%</td>
<td>1.06$x+1$</td>
</tr>
<tr>
<td>Alice Springs</td>
<td>442315</td>
<td>634</td>
<td>$+4$</td>
<td>$+1%$</td>
<td>33</td>
<td>5%</td>
<td>1.02$x-10$</td>
</tr>
<tr>
<td>Lauder</td>
<td>117090</td>
<td>544</td>
<td>$-32$</td>
<td>$-6%$</td>
<td>48</td>
<td>9%</td>
<td>0.93$x+3$</td>
</tr>
</tbody>
</table>
Europe (Palaiseau, Carpentras, Payner) and Australia (Alice Springs), while largest values are found in Xianghe (China, $-22$ W m$^{-2}$), Sede Boqer (Israel, $-48$ W m$^{-2}$), Brasilia ($+33$ W m$^{-2}$), and Lauder (New Zealand, $-32$ W m$^{-2}$). The fitting line is close to the identity line, with slopes ranging between 0.96 and 1.04, except for Xianghe (0.86) and Lauder (0.93). The RMSE is small in all cases and ranges between 0.96 and 1.04, except for Xianghe (0.86) and Lauder (0.93). The RMSE decreases with increasing $\Theta_S$ (Fig. 15). The relative bias and the relative RMSE are not constant as a function of $\Theta_S$.

The circumsolar irradiance was not taken into account to adjust $E_{\text{dir}}$ estimated by McClear to ground measurements. Pyrheliometers have an aperture angle of 5°, and therefore include part of the circumsolar radiation into the measured $E_{\text{dir}}$. This circumsolar irradiance under clear sky is less than 10 W m$^{-2}$ (Oumbe et al., 2012); it may partly explain the bias in case of underestimation.

The diffuse component $E_{\text{diff}}$ is computed by subtracting $E_{\text{dir}}$ from $E_{\text{glo}}$. Therefore, the bias in $E_{\text{diff}}$ can be computed from Tables 2 and 3. It ranges from $-8$ to $60$ W m$^{-2}$. As a whole, $E_{\text{diff}}$ is overestimated, except for Brasilia and Tamanrasset.

The bias for the clearness index $K_T$ (Table 4) ranges from $-0.017$ ($-2\%$) to $0.022$ ($3\%$). The relative RMSE comprises between 4% and 5% of the mean observed value. The squared correlation coefficients for the clearness index $K_T$ have been reported in Table 4. They should be discussed

### Table 4. Comparison between clear-sky global clearness indices measured by BSRN and estimated by McClear.

<table>
<thead>
<tr>
<th>Station</th>
<th>Number of samples</th>
<th>Mean observed value</th>
<th>Rel. bias %</th>
<th>RMSE %</th>
<th>Rel. RMSE %</th>
<th>Squared correl. coeff.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Barrow</td>
<td>70283</td>
<td>0.76</td>
<td>$-0.017$</td>
<td>$-2%$</td>
<td>0.033</td>
<td>4% 0.77</td>
</tr>
<tr>
<td>Palaiseau</td>
<td>29222</td>
<td>0.71</td>
<td>$+0.002$</td>
<td>$+0%$</td>
<td>0.029</td>
<td>4% 0.62</td>
</tr>
<tr>
<td>Carpentras</td>
<td>300468</td>
<td>0.72</td>
<td>$+0.023$</td>
<td>$+3%$</td>
<td>0.035</td>
<td>5% 0.69</td>
</tr>
<tr>
<td>Payner</td>
<td>136879</td>
<td>0.73</td>
<td>$+0.024$</td>
<td>$+3%$</td>
<td>0.037</td>
<td>5% 0.60</td>
</tr>
<tr>
<td>Xianghe</td>
<td>33795</td>
<td>0.75</td>
<td>$-0.009$</td>
<td>$-1%$</td>
<td>0.036</td>
<td>5% 0.37</td>
</tr>
<tr>
<td>Tateno</td>
<td>133433</td>
<td>0.72</td>
<td>$+0.019$</td>
<td>$+3%$</td>
<td>0.039</td>
<td>5% 0.45</td>
</tr>
<tr>
<td>Sede Boqer</td>
<td>304550</td>
<td>0.75</td>
<td>$+0.010$</td>
<td>$+1%$</td>
<td>0.032</td>
<td>4% 0.55</td>
</tr>
<tr>
<td>Tamanrasset</td>
<td>331045</td>
<td>0.79</td>
<td>$+0.013$</td>
<td>$+2%$</td>
<td>0.027</td>
<td>4% 0.71</td>
</tr>
<tr>
<td>Brasilia</td>
<td>73563</td>
<td>0.74</td>
<td>$+0.022$</td>
<td>$+3%$</td>
<td>0.032</td>
<td>4% 0.74</td>
</tr>
<tr>
<td>Alice Springs</td>
<td>442315</td>
<td>0.77</td>
<td>$+0.013$</td>
<td>$+2%$</td>
<td>0.024</td>
<td>3% 0.83</td>
</tr>
<tr>
<td>Lauder</td>
<td>117090</td>
<td>0.74</td>
<td>$+0.015$</td>
<td>$+2%$</td>
<td>0.029</td>
<td>4% 0.75</td>
</tr>
</tbody>
</table>

### Table 5. Comparison between clear-sky beam clearness indices on horizontal surface measured by BSRN and estimated by McClear.

<table>
<thead>
<tr>
<th>Station</th>
<th>Number of samples</th>
<th>Mean observed value</th>
<th>Rel. bias %</th>
<th>RMSE %</th>
<th>Rel. RMSE %</th>
<th>Squared correl. coeff.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Barrow</td>
<td>70283</td>
<td>0.61</td>
<td>$-0.040$</td>
<td>$-6%$</td>
<td>0.066</td>
<td>11% 0.55</td>
</tr>
<tr>
<td>Palaiseau</td>
<td>29222</td>
<td>0.58</td>
<td>$-0.011$</td>
<td>$-2%$</td>
<td>0.046</td>
<td>8% 0.61</td>
</tr>
<tr>
<td>Carpentras</td>
<td>300468</td>
<td>0.60</td>
<td>$-0.004$</td>
<td>$-1%$</td>
<td>0.044</td>
<td>7% 0.64</td>
</tr>
<tr>
<td>Payner</td>
<td>136879</td>
<td>0.61</td>
<td>$+0.004$</td>
<td>$+1%$</td>
<td>0.048</td>
<td>8% 0.53</td>
</tr>
<tr>
<td>Xianghe</td>
<td>33795</td>
<td>0.61</td>
<td>$-0.025$</td>
<td>$-4%$</td>
<td>0.069</td>
<td>11% 0.24</td>
</tr>
<tr>
<td>Tateno</td>
<td>133433</td>
<td>0.59</td>
<td>$-0.021$</td>
<td>$-4%$</td>
<td>0.057</td>
<td>10% 0.44</td>
</tr>
<tr>
<td>Sede Boqer</td>
<td>304550</td>
<td>0.64</td>
<td>$-0.053$</td>
<td>$-8%$</td>
<td>0.067</td>
<td>11% 0.59</td>
</tr>
<tr>
<td>Tamanrasset</td>
<td>331045</td>
<td>0.66</td>
<td>$+0.014$</td>
<td>$+2%$</td>
<td>0.043</td>
<td>7% 0.64</td>
</tr>
<tr>
<td>Brasilia</td>
<td>73563</td>
<td>0.63</td>
<td>$+0.029$</td>
<td>$+5%$</td>
<td>0.044</td>
<td>7% 0.75</td>
</tr>
<tr>
<td>Alice Springs</td>
<td>442315</td>
<td>0.67</td>
<td>$+0.002$</td>
<td>$+0%$</td>
<td>0.037</td>
<td>6% 0.75</td>
</tr>
<tr>
<td>Lauder</td>
<td>117090</td>
<td>0.66</td>
<td>$-0.035$</td>
<td>$-5%$</td>
<td>0.054</td>
<td>8% 0.72</td>
</tr>
</tbody>
</table>
with care as the limited range of values tends to decrease the correlation coefficient without denoting poor performance as discussed previously.

The bias for KTdir (Table 5) ranges from $-0.053$ (Sede Boqer, $-8\%$) to $0.029$ (Brasilia, $+5\%$). The relative RMSE comprises between $6\%$ and $11\%$ of the mean observed value.

One may note that the stations Carpentras, Payerne, Xianghe, Tateno, and Lauder have elevations below the mean MACC elevation (Table 1). No further elevation correction is applied in these cases; the elevation used for computation is the mean MACC elevation. Consequently, one may expect an overestimation of the direct component because of the theoretical underestimation of the air mass. This is not what is observed; over these 5 cases, 4 exhibit underestimation. For the time being, this effect is unnoticeable compared to remaining uncertainties in aerosol modelling as input data source.

6 Comparison with other modelled clear-sky values

Several models for assessing the SSI under clear sky can be found in the literature. They are usually validated against ground measurements as done in the present work but with a noticeable difference: inputs are atmospheric parameters taken from collocated measuring instruments. Hence these validations qualify the intrinsic performances of the model rather than its real-life performances (Gueymard, 2012; Ineichen, 2006; Mueller et al., 2004; Rigollier et al., 2000).

Schillings et al. (2004) have performed validation of their model against hourly irradiance received on a plane normal to the sun rays for 8 sites in Saudi Arabia. Clear-sky instants are defined by the values of their model. Their results cannot be directly compared to ours which have been obtained for $E_{\text{dir}}$ (horizontal surface). However, relative RMSE can be compared: it ranges from $13\%$ to $17\%$ in their case, and $7\%$ (Tamanrasset) and $9\%$ (Sede Boqer) in ours.

Greuell et al. (2013) have developed a method for the retrieval of hourly means of the SSI using Meteosat images. MACC data are inputs to their method. Comparisons were made with several BSRN stations for the year 2006 for clear-sky cases and all skies. Though the period is not similar and
Table 6. Comparison between clear-sky global irradiances on a horizontal surface measured by BSRN and estimated by HelioClim-3v3 (HC3v3, in italics) or by McClear.

<table>
<thead>
<tr>
<th>Station</th>
<th>Number of samples</th>
<th>Mean observed value W m⁻²</th>
<th>Bias W m⁻²</th>
<th>Rel. bias %</th>
<th>RMSE W m⁻²</th>
<th>Rel. RMSE %</th>
<th>Squared correl. coeff.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Palaiseau</td>
<td>HC3v3 28292</td>
<td>598</td>
<td>-1</td>
<td>-0 %</td>
<td>62</td>
<td>10 %</td>
<td>0.97</td>
</tr>
<tr>
<td></td>
<td>McClear 29222</td>
<td>598</td>
<td>+7</td>
<td>+1 %</td>
<td>25</td>
<td>4 %</td>
<td>0.99</td>
</tr>
<tr>
<td>Carpentras</td>
<td>HC3v3 298410</td>
<td>596</td>
<td>-11</td>
<td>-2 %</td>
<td>45</td>
<td>8 %</td>
<td>0.98</td>
</tr>
<tr>
<td></td>
<td>McClear 300468</td>
<td>596</td>
<td>+20</td>
<td>+3 %</td>
<td>29</td>
<td>5 %</td>
<td>0.99</td>
</tr>
<tr>
<td>Payerne</td>
<td>HC3v3 136225</td>
<td>629</td>
<td>-43</td>
<td>-7 %</td>
<td>62</td>
<td>10 %</td>
<td>0.96</td>
</tr>
<tr>
<td></td>
<td>McClear 136879</td>
<td>629</td>
<td>+23</td>
<td>+4 %</td>
<td>31</td>
<td>5 %</td>
<td>0.99</td>
</tr>
<tr>
<td>Sede Boqer</td>
<td>HC3v3 303869</td>
<td>784</td>
<td>-35</td>
<td>-4 %</td>
<td>54</td>
<td>7 %</td>
<td>0.96</td>
</tr>
<tr>
<td></td>
<td>McClear 304550</td>
<td>785</td>
<td>+12</td>
<td>+2 %</td>
<td>27</td>
<td>4 %</td>
<td>0.99</td>
</tr>
<tr>
<td>Tamanrasset</td>
<td>HC3v3 330194</td>
<td>791</td>
<td>-24</td>
<td>-3 %</td>
<td>37</td>
<td>5 %</td>
<td>0.99</td>
</tr>
<tr>
<td></td>
<td>McClear 331045</td>
<td>791</td>
<td>+8</td>
<td>+1 %</td>
<td>20</td>
<td>3 %</td>
<td>0.99</td>
</tr>
</tbody>
</table>

Table 7. Comparison between clear-sky beam irradiances on a horizontal surface measured by BSRN and estimated by HelioClim-3v3 (HC3v3, in italics) or by McClear.

<table>
<thead>
<tr>
<th>Station</th>
<th>Number of samples</th>
<th>Mean observed value W m⁻²</th>
<th>Bias W m⁻²</th>
<th>Rel. bias %</th>
<th>RMSE W m⁻²</th>
<th>Rel. RMSE %</th>
<th>Squared correl. coeff.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Palaiseau</td>
<td>HC3v3 28292</td>
<td>492</td>
<td>-14</td>
<td>-3 %</td>
<td>79</td>
<td>16 %</td>
<td>0.91</td>
</tr>
<tr>
<td></td>
<td>McClear 29222</td>
<td>492</td>
<td>-3</td>
<td>-1 %</td>
<td>37</td>
<td>7 %</td>
<td>0.96</td>
</tr>
<tr>
<td>Carpentras</td>
<td>HC3v3 298410</td>
<td>505</td>
<td>-46</td>
<td>-9 %</td>
<td>76</td>
<td>15 %</td>
<td>0.93</td>
</tr>
<tr>
<td></td>
<td>McClear 300468</td>
<td>505</td>
<td>-1</td>
<td>-0 %</td>
<td>35</td>
<td>7 %</td>
<td>0.97</td>
</tr>
<tr>
<td>Payerne</td>
<td>HC3v3 136225</td>
<td>530</td>
<td>-94</td>
<td>-18 %</td>
<td>111</td>
<td>21 %</td>
<td>0.90</td>
</tr>
<tr>
<td></td>
<td>McClear 136879</td>
<td>530</td>
<td>+6</td>
<td>+1 %</td>
<td>39</td>
<td>7 %</td>
<td>0.96</td>
</tr>
<tr>
<td>Sede Boqer</td>
<td>HC3v3 303869</td>
<td>667</td>
<td>-89</td>
<td>-13 %</td>
<td>118</td>
<td>18 %</td>
<td>0.85</td>
</tr>
<tr>
<td></td>
<td>McClear 304550</td>
<td>667</td>
<td>-48</td>
<td>-7 %</td>
<td>62</td>
<td>9 %</td>
<td>0.95</td>
</tr>
<tr>
<td>Tamanrasset</td>
<td>HC3v3 330194</td>
<td>653</td>
<td>-14</td>
<td>-2 %</td>
<td>87</td>
<td>13 %</td>
<td>0.86</td>
</tr>
<tr>
<td></td>
<td>McClear 331045</td>
<td>653</td>
<td>+16</td>
<td>+2 %</td>
<td>48</td>
<td>7 %</td>
<td>0.95</td>
</tr>
</tbody>
</table>

comparisons were made on an hourly basis rather than 1 min, performances can be compared for the bias for the three common sites: Palaiseau, Carpentras, and Payerne. Both models provide similar results for both \( E_{\text{glob}} \) and \( E_{\text{dir}} \).

The SoDa Web site (www.soda-is.org) provides SSI from the database HelioClim-3v3 (HC3v3, Blanc et al., 2010; Espinar et al., 2012). The HelioClim database derives from images of the Meteosat series of satellites using the Heliosat-2 method (Rigollier et al., 2004) and the ESRA clear-sky model (Wald et al., 2000; Rigollier et al., 2000) modified by Geiger et al. (2002) with the climatology of the Linke turbidity factor from Remund et al. (2003) as inputs. The Linke turbidity factor is a convenient approximation to model the atmospheric absorption and scattering of the solar radiation under clear sky. The climatology of Remund et al. (2003) comprises 12 maps, one per month, covering the world by cells of 5° of arc angle in size. The SoDa Service is able to provide 1 min \( E_{\text{glob}} \) which is compared to that from BSRN for the clear-sky instants and the stations in the field-of-view of Meteosat: Palaiseau, Carpentras, Payerne, Sede Boqer, and Tamanrasset.

Tables 6 and 7 report bias, RMSE and squared correlation coefficient for HC3v3 and McClear respectively. It appears clearly than the performances of McClear are much better than those of HC3v3. Knowing that HC3v3 is exploited by many companies and researchers in solar energy – approximately 2 million time series of HC3v3 were supplied by the SoDa Service in 2011 – one may measure the strong interest in McClear in this community.

7 Conclusions

The new clear-sky model McClear exhibits very satisfactory results as a fast implementation of radiative transfer theory for the direct and global irradiance. The comparison between McClear estimates and measurements of global and beam SSI for 11 stations in the world shows that a large correlation is attained. For 1 min averages of global irradiance, the correlation coefficient ranges between 0.95 and 0.99. The bias comprises between -6 and 25 W m⁻², and the RMSE between 20 W m⁻² (3 % of the mean observed
irradiance) and 36 W m\(^{-2}\) (5\%). For direct irradiance, the correlation coefficient ranges between 0.84 and 0.99. The bias comprises between −48 and 33 W m\(^{-2}\), and the RMSE between 33 W m\(^{-2}\) (5\% of the mean observed irradiance) and 64 W m\(^{-2}\) (10\%). As a whole, 95\% of the deviations are less than approximately 50 W m\(^{-2}\) for global and 70 W m\(^{-2}\) for direct irradiance.

Comparisons with state-of-the-art clear-sky models show that McClear offers similar or better performances. These very good results demonstrate the quality of the McClear model and indirectly the quality of the aerosol properties modelled by the MACC reanalysis.

Performances are still far from WMO standards: bias less than 3 W m\(^{-2}\) and 95\% of the deviations less than 20 W m\(^{-2}\). Uncertainties in aerosol properties from MACC are still too large, and more efforts are necessary for a better modelling of the aerosols.

The novelty of the McClear model is the inclusion of variable aerosol optical properties, water vapour, and ozone with a high update frequency of 3 h compared to the previously used monthly climatologies in clear-sky models. The large correlation coefficient and the low standard deviation, computed from the RMSE and bias, demonstrate that McClear offers accurate estimates of changes in time of the SSI.

Since MACC provides also forecasts of the aerosol properties and ozone, and various meteorological services provide forecasts of water vapour from any NWP centre, McClear can also be used for forecasting of clear-sky irradiances in future.

The McClear model with inputs from MACC and MODIS is available as a Web service, i.e. an application that can be invoked via the Web. It obeys the OGC (Open Geospatial Consortium) standard for Web processing services (WPS) (Percival et al., 2011). An interface has been developed to launch McClear within a standard Web browser and to obtain time series of global and beam SSI under clear sky for a given point and a given period for the following summarizations: 1 min, 15 min, 1 h and 1 day. This interface can be launched via the catalogue of products on the MACC Web site (www.macc-atmosphere.eu).

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References


