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Towards Compositional and Generative Tensor Optimizations
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Tensors in Computational Fluid Dynamics (CFD)
- Loop characteristics:
  - 3 to 4 dimensions nesting
  - Few iterations per dimension (e.g., 17 or 33 iterations)
- Type of computations:
  - Tensor contractions
  - Outer products
  - Element-wise multiplications
  - Computations on each element of a structured mesh

Inverse Helmholtz
\[
 t_{ijk} = \sum_{l,m,n} A_{kn}^T \cdot A_{jm}^T \cdot A_{il}^T \cdot \Omega_{lmn} \\
p_{ijk} = D_{ijk} \cdot t_{ijk} \\
v_{ijk} = \sum_{l,m,n} A_{kn} \cdot A_{jm} \cdot A_{il} \cdot p_{lmn}
\]

Tensor Optimization Frameworks
- Domain-specific expressivity
- Flexible/Adaptive optimization heuristics
- Hidden and/or rigid optimization heuristics

Related Work
- Different levels of expressiveness and control on optimizations
  - Flexible/adaptive
  - Hidden/rigid

Optimizing CFD Kernels with Existing Tools
- Several limitations
- Few opportunities for adaptations

Goal
A cross-domain intermediate language for tensor optimizations

Intermediate Language
- Modular constructs
- First-class citizens:
  - Arrays
  - Tensor operators
  - Loop iterators
  - Transformations

Envisioned Tool
- Intermediate language
- Meta-programming
- Iterative search

Search Space Exploration
- Evaluation order of tensor contractions
- Fusions
- Permutations
- Vectorization
- Collapsing
- Unrolling

Inverse Helmholtz by Example

# Basic array declaration
A = array(2, double, [N, N])
u = array(3, double, [N, N, N])
D = array(3, double, [N, N, N])

# Transposition
At = vtranspose(A, 1, 2)

# Tensor contractions
tmp1 = contract(At, u, [2, 1])
tmp2 = contract(At, tmp1, [2, 2])
tmp3 = contract(At, tmp2, [2, 3])
tmp4 = entrywise(D, tmp3)

# Tensor contractions
tmp5 = contract(A, tmp4, [2, 1])
tmp6 = contract(A, tmp5, [2, 2])

# Iterator declaration
i1 = iterator(0, N, 1)
i2 = iterator(0, N, 1)

# Association of iterators to computations
build(D, [td1, td2, td3])
build(tmp1, [i1, i2, i3, i4])
build(tmp5, [i1, i2, i3, i4])
build(tmp6, [k12, k22, k32, k42])

# Loop interchanges
 interchange(i4, i3)
 interchange(i4, i2)
 interchange(j2, j1)
 interchange(j1, j4)

# Transpositions
tmp2t = vtranspose(tmp2, 1, 2)
replace_array(j3, tmp2, tmp2t)
replace_array(k4, tmp3, tmp3t)
interchange(k3, k2)

Example of assessment: Different heuristics of loop interchanges (+ parallelization)

Future Work
- Applications to other domains
- Syntax refinement
- Formal semantics

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