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Towards Compositional and Generative Tensor Optimizations

Adilla Susungi, Norman A. Rink, Jerónimo Castrillón, Immo Huismann, Albert Cohen, Claude Tadonki, Jörg Stiller and Jochen Fröhlich

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Tensors in Computational Fluid Dynamics (CFD)

- Loop characteristics:
  - 3 to 4 dimensions nesting
  - Few iterations per dimension (e.g., 17 or 33 iterations)
- Type of computations:
  - Tensor contractions
  - Outer products
  - Element-wise multiplications
  - Computations on each element of a structured mesh

Inverse Helmholtz

\[ t_{ijk} = \sum_{l,m,n} A_{kn}^T \cdot A_{jm}^T \cdot A_{il} \cdot u_{lmn} \]

\[ p_{ijk} = D_{ijk} \cdot t_{ijk} \]

\[ v_{ijk} = \sum_{l,m,n} A_{kn} \cdot A_{jm} \cdot A_{il} \cdot p_{lmn} \]

Tensor Optimization Frameworks

- Domain-specific expressivity
- Flexible/Adaptive optimization heuristics
- Hidden and/or rigid optimization heuristics

Optimizing CFD Kernels with Existing Tools

- Several limitations
- Few opportunities for adaptations

A cross-domain intermediate language for tensor optimizations

Intermediate Language

- Modular constructs
  - First-class citizens:
    - Arrays
    - Tensor operators
    - Loop iterators
    - Transformations

Envisioned Tool

- Meta-programming
- Iterative search

Search Space Exploration

- Evaluation order of tensor contractions
- Fusions
- Permutations
- Vectorization
- Collapsing
- Unrolling

Inverse Helmholtz by Example

Example of assessment: Different heuristics of loop interchanges (+ parallelization)

Baseline: sequential execution (3.32s). Machine: 24-core Intel(R) Xeon(R) CPU E5-2680 v3 @ 2.50GHz (Haswell)

Future Work

- Applications to other domains
- Syntax refinement
- Formal semantics

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Related Work

Different levels of expressiveness and control on optimizations

Flexible/adaptive

Hidden/rigid

Specific

Generic

Chill

Pluto

TensorFlow

TVM

Tensor Contraction Engine

Numpy

Tensor Algebra Compiler

Optimizing CFD Kernels with Existing Tools

Specific

Generic

Hidden/rigid

Flexible/adaptive

Optimizing CFD Kernels with Existing Tools

Several limitations

Few opportunities for adaptations

Unadapted constructs

Unadapted heuristics

Limited optimizations

Limited expressivity

Should we create yet another domain-specific solution?