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### ► To cite this version:

Pierre-Olivier Bouchard, Victor-Manuel Trejo-Navas, Modesar Shakoor, Thilo F. Morgeneyer, Ante Buljac, et al.. Recent advances in the finite element modelling of ductile fracture at mesoscale. Procedia Manufacturing, 2018, 15, pp.39-45. 10.1016/j.promfg.2018.07.167 . hal-01858266

**HAL Id: hal-01858266**

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Submitted on 28 Aug 2018

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17th International Conference on Metal Forming, Metal Forming 2018, 16-19 September 2018,  
Toyohashi, Japan

## Recent advances in finite element modelling of ductile fracture at mesoscale

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### Abstract

This work addresses ductile fracture at the meso-scale by accounting for the influence of particles on nucleation, growth and coalescence mechanisms for complex loading paths. A finite element approach was developed to model and study 3D heterogeneous microstructures with interfaces defined by level-set functions and the use of a body fitted mesh adaption technique. Specific developments were also carried out in order to model failure mechanisms occurring both during the nucleation and the coalescence stages. Initial 3D microstructures of nodular graphite cast iron are obtained from X-ray laminography pictures. In-situ tensile tests with varying stress states are carried out and nucleation, growth and coalescence mechanisms are observed. Digital volume correlation is used to access to 3D displacement (and strain) field in the bulk. These data are also used to prescribe exact boundary conditions on the faces of the finite element domain. The finite element approach therefore enables to study strain and stress states in critical areas and aims at improving the understanding of coalescence mechanisms (internal necking of the intervoid ligament or void-sheet mechanism) by comparing finite element simulations with experimental observations and digital volume correlation results. This finite element approach is used to conduct a parametric study on the relative position of three voids on void growth and coalescence modes. It is shown that 2D views of coalescence mechanisms may sometimes be misleading.

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Peer-review under responsibility of the scientific committee of the 17th International Conference on Metal Forming.

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*Keywords:* Ductile fracture; Micro-scale; Finite element; Level-set function; Mesh adaption

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## 1. Introduction

Predicting and avoiding ductile fracture during metal forming processes is still a very hot and open scientific topic despite the tremendous efforts of the metal forming community. This is due to the complexity of the thermomechanical and metallurgical mechanisms occurring during forming processes (large plastic strains under multiaxial and non-proportional loading conditions). At the macroscopic scale, the prediction of ductile fracture is usually addressed using uncoupled failure criteria, coupled continuum damage mechanics approaches or damage models based on porous-plasticity theory (see Ref. [1] for a comparison of such approaches for cold metal forming applications). These approaches do not explicitly account for the material microstructure and phenomena such as the influence of particles (nature, shape, orientation and distribution) on damage anisotropy or nucleation/coalescence mechanisms cannot be properly addressed. However, it has been shown that such a microstructure can have a direct impact on damage mechanisms [2].

This work studies ductile damage issues at mesoscale, where particles and voids are considered and meshed in 2D and 3D volumes. In order to understand the underlying physical mechanisms for complex loading paths, three modern techniques are seamlessly coupled: (i) X-ray laminography to image in situ tested large flat samples made of ductile materials [3], (ii) digital volume correlation to measure 3D displacement (and strain) fields in the bulk [4], and (iii) 2D/3D finite element simulations using the experimental information on multiple length-scales [5-7]. First, the finite element methodology developed to model void nucleation, growth and coalescence mechanisms is described. The overall strategy is then presented through applications on nodular graphite cast iron. Finally a numerical sensitivity analysis is conducted to study the influence of the position of three voids on coalescence mechanisms.

## 2. Finite element methodology

The studied domains are 2D or 3D Representative Volume Elements generally composed of a matrix, particles, and voids. A specific body-fitted mesh adaption technique was developed in [5] so as to preserve the geometric properties of level-set functions as well as the volume and morphology of each component of the microstructure, even at large plastic strains. A particularity of the present framework is that voids are also meshed, meaning that there are mesh elements inside cracks. These elements are only used for remeshing purposes, and measurement of void volume fraction, but have no stiffness or constitutive behavior. Their effect is hence no different than actual voids (that would not be meshed). The matrix is defined by an elastic-plastic behavior and particles are assumed to be elastic brittle. They are assumed to debond or fail before yielding can occur. Both nucleation mechanisms are based on local stress-based criteria that are described in details in [8]. Fig. 1 shows an example where a microstructure containing several particles is submitted to tension. Void nucleation by debonding (for example top-left corner) and by particles failure (right side) can be observed up to 50% of elongation.

Coalescence is characterized by the initiation of micro-cracks between voids leading to final fracture. From a numerical point of view, such coalescence mechanism can be modelled naturally by internal necking in the intervoid ligament when level-set functions get in contact and merge. If a mechanical criterion (to be defined) is reached in the intervoid ligament, it is also possible to propagate a straight crack from one void to another. Void coalescence will be studied in section 4 and more details can be found in [5, 9].

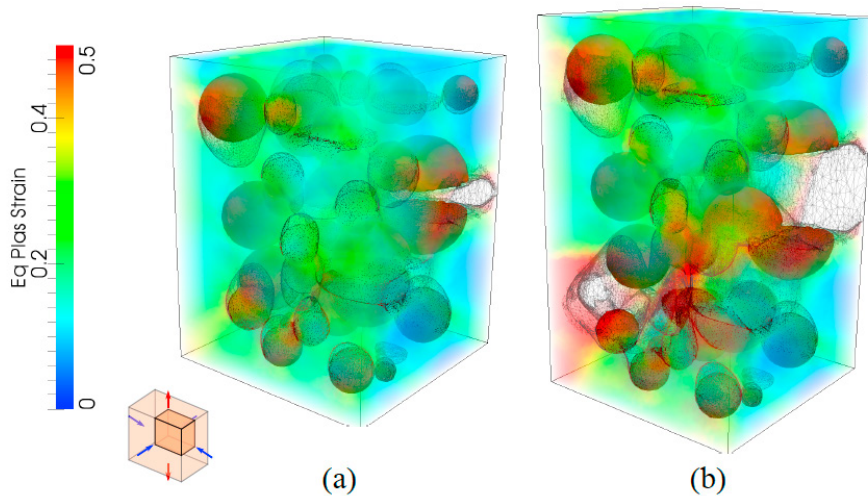


Fig. 1. Equivalent plastic strain for 3D microstructure under tensile loading with both nucleation mechanisms activated at Representative Volume Elements elongation of (a) 25% and (b) 50% (from [8]).

### 3. Application to nodular cast iron

The studied material is a commercial nodular graphite cast iron (specimens supplied by M. Kuna, L. Zybell and M. Horn from TU Bergakademie Freiberg). At the microscale, this material exhibits a ferritic steel matrix and graphite nodules. Under tensile loading, ductile fracture is mainly driven by a very early debonding of the nodules from the matrix, and coalescence of the subsequent nucleated voids [10]. Due to their very low load carrying capacity under tensile loading, it is suggested [10] to model such nodules as voids. With this simplifying assumption, the material is considered as a two-phase microstructure with an elastic-plastic ferritic matrix and voids.

In order to study the growth and coalescence stage, a specific methodology has been developed. This methodology is based on the following steps:

- Acquisition of the real initial 3D microstructure based on X-Ray laminography [3]. These pictures are taken from a region located at the center of a flat tensile specimen with two holes machined at 45° with respect to the loading direction. These pictures are also recorded at different stages of the tensile test so as to observe coalescence mechanisms.
- Global DVC to measure displacement fields whose kinematic basis is made of the shape functions of 8-noded elements [11]. The digital volume correlation registration technique used to measure 3D displacement fields in the bulk of samples is based on a global approach [12] which consists in minimizing gray level residuals on the whole region of interest and in using kinematic fields based on FE discretizations.
- Meshing of the real initial microstructure (two-phase material) of a domain included in the region of interest and application of boundary conditions coming from the digital volume correlation step.

The whole methodology is presented in detail in [6].

Based on this approach, it is possible to study void growth and strain increase in the ferritic matrix both using digital volume correlation data and finite element simulations. Regarding finite element simulations, note that applying the exact digital volume correlation boundary condition is really important compared to classical finite element multiscale strategies, as explained in [7]. Fig. 2 shows a 2D cut of the region of interest at different stages of the tension test. Fig. 2(a) is a superimposition of the finite element strain field and the microstructure at  $t_0$ . Fig. 2(b) and Fig. 2(c) show a superimposition of the von Mises strain field at  $t_1$  obtained respectively by digital volume correlation and finite element calculations. These strain localizations are in good agreement with the failure path

observed at the last stage before complete fracture illustrated in Fig. 2d (at  $t_f$ ). Note that localization bands are described better due to a finer finite element mesh than the digital volume correlation mesh.

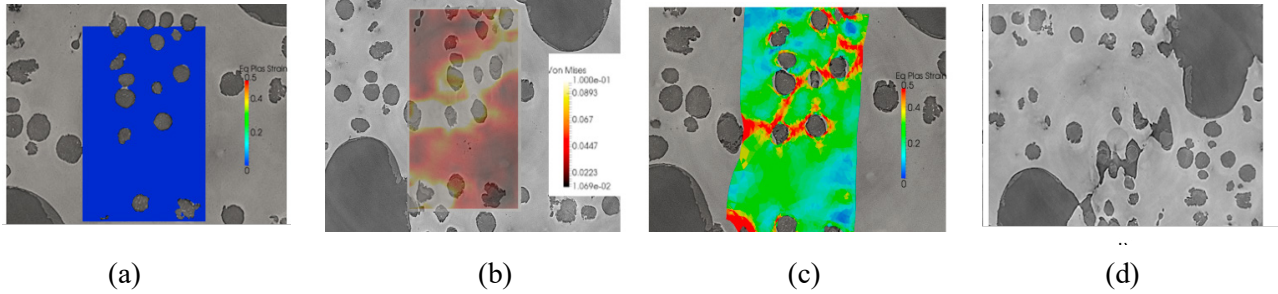


Fig. 2. Observation of void growth and coalescence on 2D cut of the region of interest at different stages of tension test and superimposition of digital volume correlation and finite element equivalent strain field on microstructure.

The observations from X-Ray laminography enable to exhibit the two main coalescence mechanisms. The most observed coalescence mode is due to internal necking between neighboring voids with plastic localization in the intervoid ligaments. For lower stress triaxiality ratios, a shear driven localization mode, often called void-sheet coalescence, can also be observed. This void-sheet coalescence mode is not yet perfectly understood. In [13], digital volume correlation analyses were conducted in areas corresponding to these two coalescence mechanisms. These analyses showed that the equivalent strain reached at the last stage before failure was approximately the same for the two different coalescence mechanisms. However, it must be noted that void-sheet coalescence is usually observed in 2D micrographs or 2D X-ray tomography pictures without accounting for the influence of other voids possibly located deeper in the material. In order to study the influence of such 3D effect, a numerical parametric study is conducted in the next section.

#### 4. Void coalescence analysis

##### 4.1. Influence of voids position on coalescence

In the following, a 3D cubic domain containing three spherical voids is considered. The size of the domain is large enough to assure negligible interaction with the boundaries. The domain, illustrated in Fig. 3(a), is submitted to tension in the vertical  $y$  direction by applying a normal velocity  $V_y$  up to a vertical strain  $E_{yy}$  equal to 0.5. Symmetry conditions, indicated by red arrows, are used on three faces of the domain. Finally, on the two remaining faces, velocities are prescribed so as to respect a given stress state (stress triaxiality ratio equals 1 and Lode angle is fixed to 0.34 in the following). The matrix is assumed to be elastic perfectly plastic. Three voids (radius = 50  $\mu\text{m}$ ) are located at the center of the domain (See Fig. 3(b)). The two external voids centers are placed at  $z = 0$ . They are positioned at  $45^\circ$  with respect to the loading direction. The distance between the center of the domain (noted  $O$ ) and their closest surface is noted  $d1$ . The third void, named internal void, is centered along the  $x$  and  $y$  axes ( $y = 0$  and  $x = 0$ ) and its position varies along  $z$ .  $d2$  denotes the distance between the center of the domain and its closest surface. For the sake of simplicity,  $d1$  and  $d2$  will be normalized by the voids radius  $R$  in the following. The sensitivity analysis is conducted with  $d1$  varying between 1 and 3.25 and  $d2$  varying between 1 and 4. For each configuration, the minimum intervoid distance, normalized void volume and equivalent plastic strain at the center between voids (see Fig. 3(c)) can be plotted.

In the following, the results will be shown for  $d1 = 1$  and for  $d2$  varying between 1 and 4. For the complete analysis of the domain space, the reader can refer to [9]. Fig. 4 shows external-external and internal-external distances evolution for three different values of  $d2$ .

For  $d2 = 1$  (Fig. 3(a)), the distance between the two external voids is twice the one between external voids and the internal void. The decrease of this distance is similar and coalescence arises when the internal-external voids distance reaches zero for a strain value close to 0.12.

When  $d_2$  is increased to 3.25 (Fig. 3(b)), the internal-external distance is higher at the beginning but its decrease is faster than the external-external one. Again, coalescence occurs between external voids and the internal one. It is interesting to notice the acceleration of the decrease at the end just before coalescence occurs.

Finally, when  $d_2$  is increased to 4 (Fig. 3(c)), both curves exhibit a fast decrease at the end with coalescence occurring between the two external voids first and almost instantaneously between the internal and the two external voids.

It is also interesting to notice that increasing the  $d_2$  distance from 1 to 4 leads to an increase of the equivalent strain at coalescence from 0.12 to 0.43. The complete sensitivity analysis, presented in [9], enables to plot the coalescence strain as a function of  $d_1$  and  $d_2$ .

For each configuration, a view of the 3 voids at the onset of coalescence is shown in Fig. 3. The shape of the elongated voids depends on the initial configuration and the presence of the internal void clearly influences these coalescence mechanisms. In order to investigate further this influence an analysis is conducted with and without the presence of the internal void in the next section.

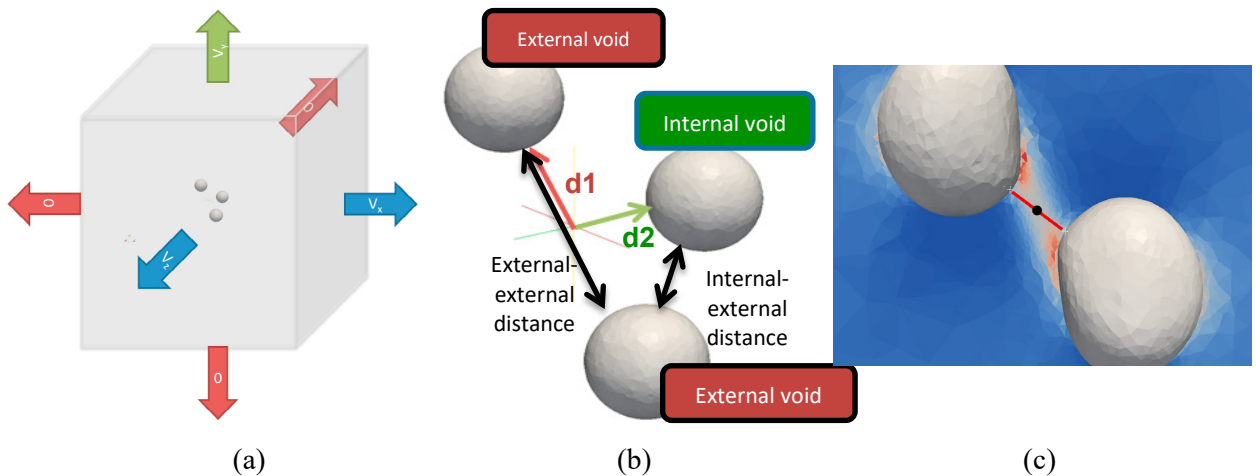


Fig. 3. (a) 3D domain with prescribed boundary conditions; (b) relative position between two external voids and internal void; (c) localization of sensor for strain analysis.

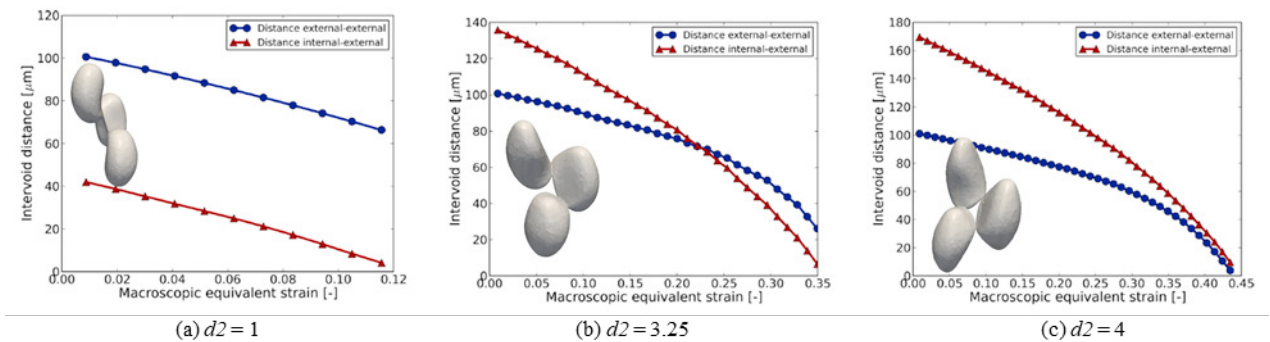


Fig. 4. Plot of external-external and internal-external distances for  $d_1 = 1$  and 3 different values of  $d_2$ .



#### 4.2. Effect of internal void on void growth and coalescence mechanism

In order to study the influence of an internal void on void growth and coalescence mechanisms, two simulations were conducted. The first simulation accounted for the two external voids only, at a normalized distance  $d2 = 1$ . The second simulation was identical, but with the presence of an internal void at a normalized distance  $d1 = 1$ .

The analysis showed that the presence of the internal void influences significantly void growth with a faster void volume fraction than in the presence of 2 external voids only. In such a configuration, the use of a Rice & Tracey void growth model would underestimate void growth, as shown in [9].

In addition, it is interesting to observe the coalescence modes obtained for these two configurations. Fig. 5(a) (resp. Fig. 5(b)) shows the voids shape at coalescence for the configuration with two voids (resp. 3 voids). In the configuration with 3 voids it can be noticed that coalescence occurs between the internal and the two external voids simultaneously. Fig. 5(c) shows the equivalent plastic strain field in a 2D view just prior to coalescence for the 3 voids configuration. The strain localization observed here is due to the internal necking occurring between the internal void and the two external voids. For this same 3 voids configuration, Fig. 5(d) shows a 2D view of the void volume fraction just after coalescence occurs. With such a 2D view, one would conclude that coalescence occurs by void-sheeting, whereas the full 3D analysis conducted here demonstrates that this coalescence is due to internal necking between the internal void and the two external voids.

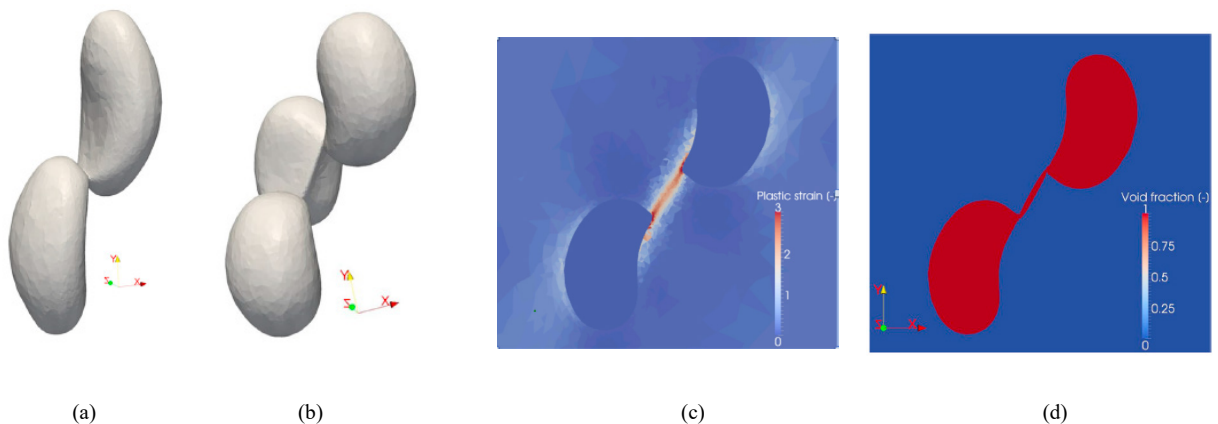


Fig. 5. Voids shape at onset of coalescence for (a) 2 voids and (b) 3 voids. (c) Equivalent plastic strain for 3 voids configuration plotted in 2D view just prior to coalescence and (d) void volume fraction for 3 voids configuration plotted in 2D view just after coalescence occurred.

## 5. Conclusion

The new FE methodology presented here enables to mesh 3D heterogeneous microstructures and to study voids nucleation, growth and coalescence for large plastic strain. Initial meshes are based on X-Ray laminography pictures for a nodular graphite cast iron. A global digital volume correlation approach was developed to study displacement (and strain) fields in the bulk thanks to the gray level of laminography pictures taken at different stages of tensile tests. These digital volume correlation fields can also be used to prescribe exact boundary conditions for finite element calculations on the real microstructure. Such an approach was conducted for the first time in [6] and the influence of boundary conditions on void growth was studied in [7].

Particular attention was paid here to the coalescence modes observed experimentally for these in-situ tension experiments on nodular cast iron. 2D views usually used to observe such failure mechanisms show both internal necking and void-sheet coalescence modes. However, such a material exhibits a very high density of nodules and, in some cases, what looks like void-sheet coalescence may actually come from the presence of other nodules or voids in the depth. To figure out the influence of such 3D effects, a parametric study was conducted with two external voids in the same plane and with the presence of a third void in the depth. This study showed that, for specific

configurations, 2D views may be misleading since they show void-sheeting coalescence mode (Fig. 5(d)) whereas coalescence is due to the presence of the third void in the depth and to plastic localization and internal necking between this third void and the two first ones (Fig. 5(b)).

However, it must be noted that this sensitivity analysis was conducted here for an elastic-plastic material with no hardening. Hardening would undoubtedly slow down plastic localization. It would therefore be interesting to confirm these results with a matrix exhibiting hardening. The variation of the stress state would also be interesting for further investigations.

## Acknowledgements

This work was performed within the COMINSIDE project funded by the French Agence Nationale de la Recherche (ANR-14-CE07-0034-02 grant). We also acknowledge the European Synchrotron Radiation Facility for provision of beamtime at beamline ID15, experiment ME 1366. It is also a pleasure to acknowledge the support of BPI France (DICCIT project), and of the Carnot M.I.N.E.S institute (CORTEX project).

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